

Physics:

$\vec{A}$ direction
sense
 $\vec{A} = A_x \hat{i} + A_y \hat{j}$

Vectors:

$\vec{v} = [\hat{i}, \hat{j}, \hat{k}]$

Addition
Subtraction
Multiplication
Cross product:

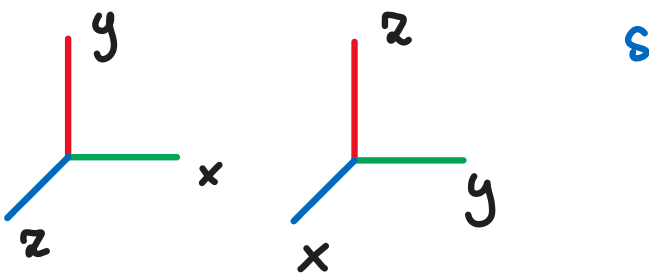
Length:

$|\vec{v}| = \sqrt{\hat{i}^2 + \hat{j}^2 + \hat{k}^2}$

$\vec{a} \times \vec{b} \neq \vec{b} \times \vec{a}$

$a = [a_x, a_y, a_z]$

$b = [b_x, b_y, b_z]$



$\vec{c} \perp \vec{a} \wedge \vec{c} \perp \vec{b}$

$\vec{c} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ a_x & a_y & a_z \\ b_x & b_y & b_z \end{vmatrix} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ a_y b_z - a_z b_y \\ a_z b_x - a_x b_z \\ a_x b_y - a_y b_x \end{vmatrix}$

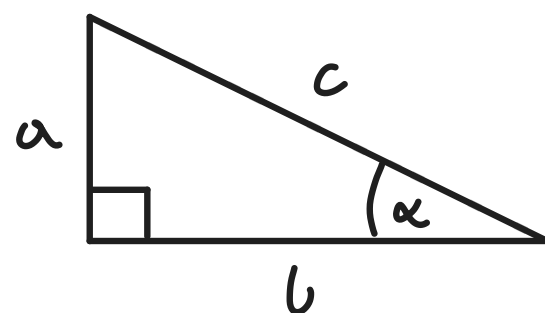
$\vec{a} \cdot \vec{b} = |\vec{a}| |\vec{b}| \cos(\vec{a}, \vec{b})$

Errors:

absolute error: $\overline{I_R} - \overline{I_C} = \Delta I$
real number estimation

relative error: $\frac{\Delta I}{\overline{I_C}} = f$

Trigonometry



$\sin \alpha = \frac{a}{c}$ $\tan \alpha = \frac{a}{b}$

$\cos \alpha = \frac{b}{c}$ $\cot \alpha = \frac{b}{a}$

$\sin^2 \alpha + \cos^2 \alpha = 1$

$1 + \tan^2 \alpha = \frac{1}{\cos^2 \alpha}$

$1 + \cot^2 \alpha = \frac{1}{\sin^2 \alpha}$

$\sin(-\alpha) = -\sin \alpha$

$\cos(-\alpha) = \cos \alpha$

$\tan(-\alpha) = -\tan \alpha$

Motion:

$v = \frac{s}{t} \quad | \quad s = vt \quad | \quad t = \frac{s}{v}$

relative speed:

$\xrightarrow{v_1} \quad \xleftarrow{v_2} \quad v_R = v_1 + v_2$
 $\xrightarrow{v_1} \quad \xrightarrow{v_2} \quad v_R = v_1 - v_2$

average:

- speed $\frac{\text{total distance}}{\text{total time}}$

- velocity $\frac{\text{displacement}}{\text{total time}}$

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$\sin(\alpha \pm \beta) = \sin \alpha \cos \beta \pm \sin \beta \cos \alpha$

$\cos(\alpha \pm \beta) = \cos \alpha \cos \beta \mp \sin \alpha \sin \beta$

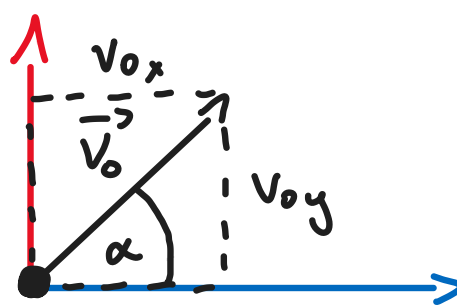
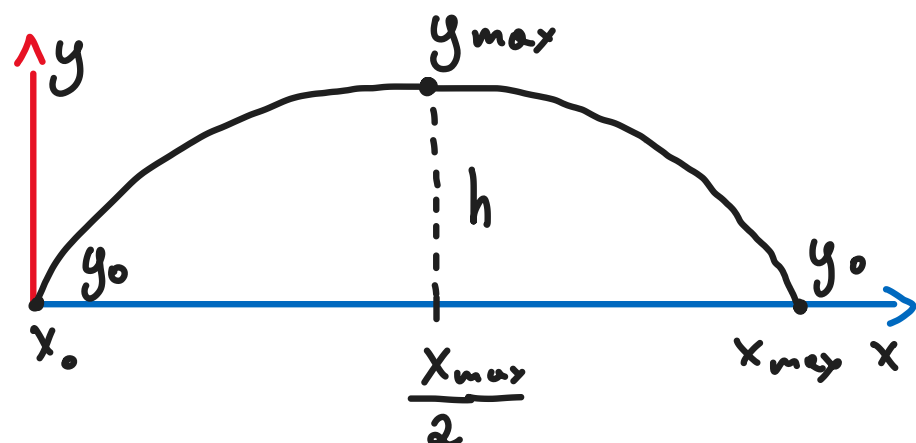
$\sin(2\alpha) = 2 \sin \alpha \cos \alpha$

$\cos(2\alpha) = \cos^2 \alpha - \sin^2 \alpha = 2 \cos^2 \alpha - 1 = 1 - 2 \sin^2 \alpha$

$x(t) = x_0 + v_0 t + \frac{at^2}{2}$

$v(t) = v_0 + at$

throwing:



initial velocity:

$\vec{v}_0 = [v_0 \cos \alpha, v_0 \sin \alpha]$

$h = \frac{v_0^2 \sin^2 \alpha}{2g} \quad [y_{\max}]$

$r(t) = [v_0 \cos \alpha t; v_0 \sin \alpha t - \frac{gt^2}{2}]$

$v(t) = [v_0 \cos \alpha; v_0 \sin \alpha - gt]$