

Digital Circuits Theory - Laboratory						
Academic year	Laboratory exercises on	Mode of studies	Field of studies	Supervisor	Group	Section
2024/2025	Wednesday	SSI	Informatics	DP	1	1
	11:45 – 13:15					

## Report from Exercise No 12

Performed on: 18.12.2024

Exercise Topic: Microprogrammable circuits

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# Introduction

introduction here

## Task 1

Obtain Mod 15 adding counter.

## Solution

We started by creating table of memory content.

$Q_3^n$	$Q_2^n$	$Q_1^n$	$Q_0^n$	$Q_3^{n+1}$	$Q_2^{n+1}$	$Q_1^{n+1}$	$Q_0^{n+1}$
$A_3$	$A_2$	$A_1$	$A_0$	$Y_3$	$Y_2$	$Y_1$	$Y_0$
0	0	0	0	0	0	0	1
0	0	0	1	0	0	1	0
0	0	1	0	0	0	1	1
0	0	1	1	0	1	0	0
0	1	0	0	0	1	0	1
0	1	0	1	0	1	1	0
0	1	1	0	0	1	1	1
0	1	1	1	1	0	0	0
1	0	0	0	1	0	0	1
1	0	0	1	1	0	1	0
1	0	1	0	1	0	1	1
1	0	1	1	1	1	0	0
1	1	0	0	1	1	0	1
1	1	0	1	1	1	1	0
1	1	1	0	1	1	1	1
1	1	1	1	0	0	0	0

Figure 1 - Table of memory content.

Next we connected basic circuit and manually programmed memory.

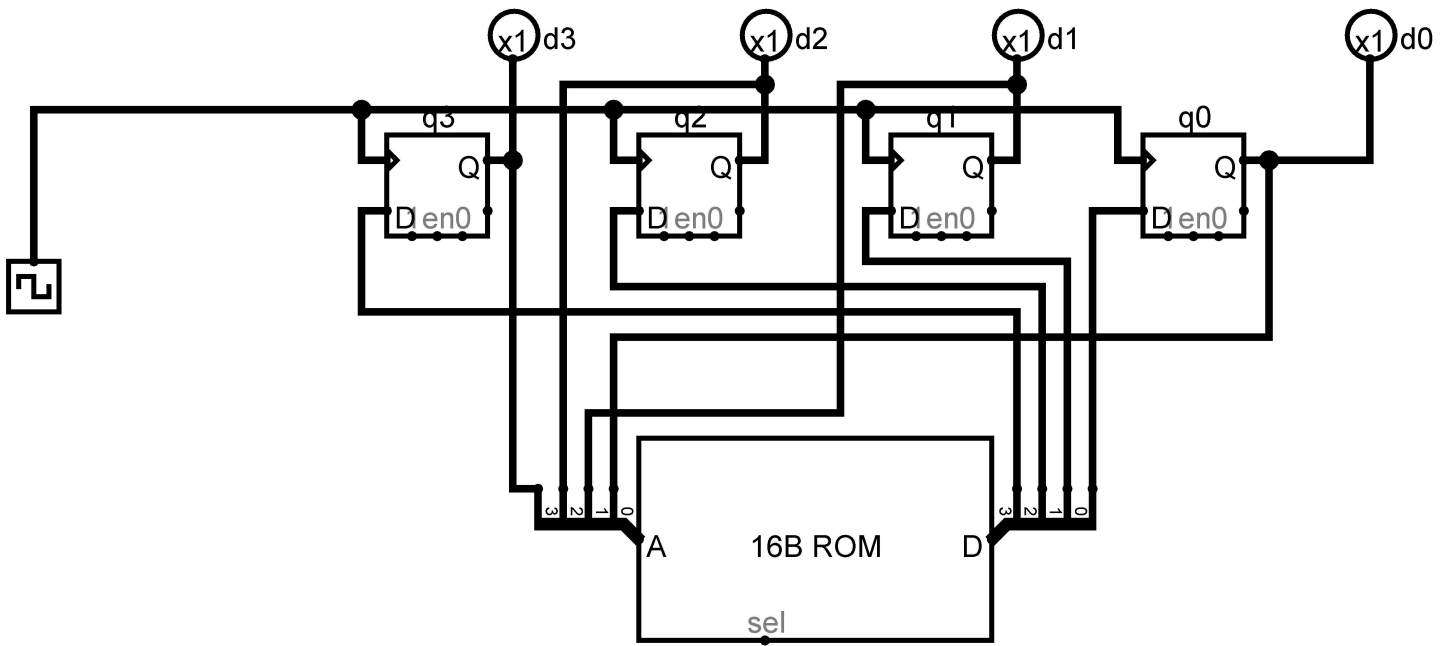
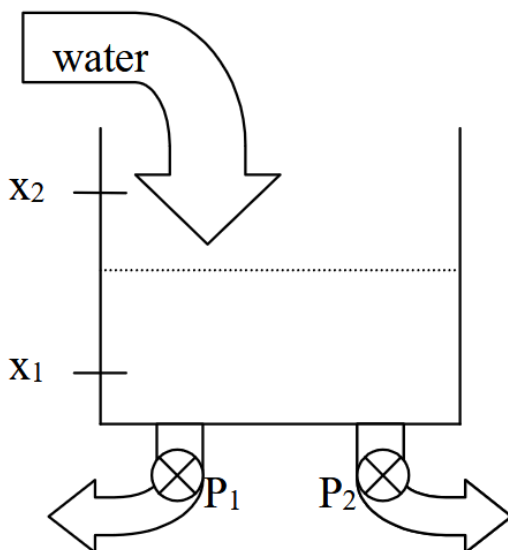


Figure 2 - Implementation of Mod 15 counter.

## Task 2

Implement as a microprogrammable circuit a system controlling the task of emptying the water container with two pumps. The pumps  $P_1$  and  $P_2$  should be switched on alternately (only one pump can work at a time) when water exceeds the level of the sensor  $x_2$  (i.e. when  $x_2 = 1$ ). Working pump should be switched off when the water lever is below the sensor  $x_1$  (i.e. when  $x_1 = 0$ ). Assume that water level grows when pumps are off, and that it decreases when any pump is working.



For the microprogrammable circuit obtain:

**a) Universal Structure**

**b) Conditional Multiplexer-based Structure**

## Solution

A primitive flow map was constructed to identify system states and transitions based on sensor inputs.

Present State	$x_1 x_2$				$P_1$	$P_2$
	00	01	11	10		
1			$\textcircled{S_0}$	$S_1$	1	0
2	$S_2$			$\textcircled{S_1}$	1	0
3	$\textcircled{S_2}$			$S_3$	0	0
4			$S_4$	$\textcircled{S_3}$	0	0
5			$\textcircled{S_4}$	$S_5$	0	1
6	$S_6$			$\textcircled{S_5}$	0	1
7	$\textcircled{S_6}$			$S_7$	0	0
8			$S_0$	$\textcircled{S_7}$	0	0

**Figure 3 - States flow map**

We reduced states as following:

$$S_0 \rightarrow S_1$$

$$S_2 \rightarrow S_3$$

$$S_4 \rightarrow S_5$$

$$S_6 \rightarrow S_7$$

Present State \ $x_1x_2$		$x_1x_2$				$P_1 P_2$	
		00	01	11	10		
$S_0$	$S_2$			$S_0$	$S_0$	1	0
$S_2$	$S_2$			$S_4$	$S_2$	0	0
$S_4$	$S_6$			$S_4$	$S_4$	0	1
$S_6$	$S_6$			$S_0$	$S_6$	0	0
		Next State					

**Figure 4 - Karnaugh map used to obtain memory content.**

We encoded states as following:

$$S_0 = 00$$

$$S_1 = 01$$

$$S_4 = 11$$

$$S_6 = 10$$

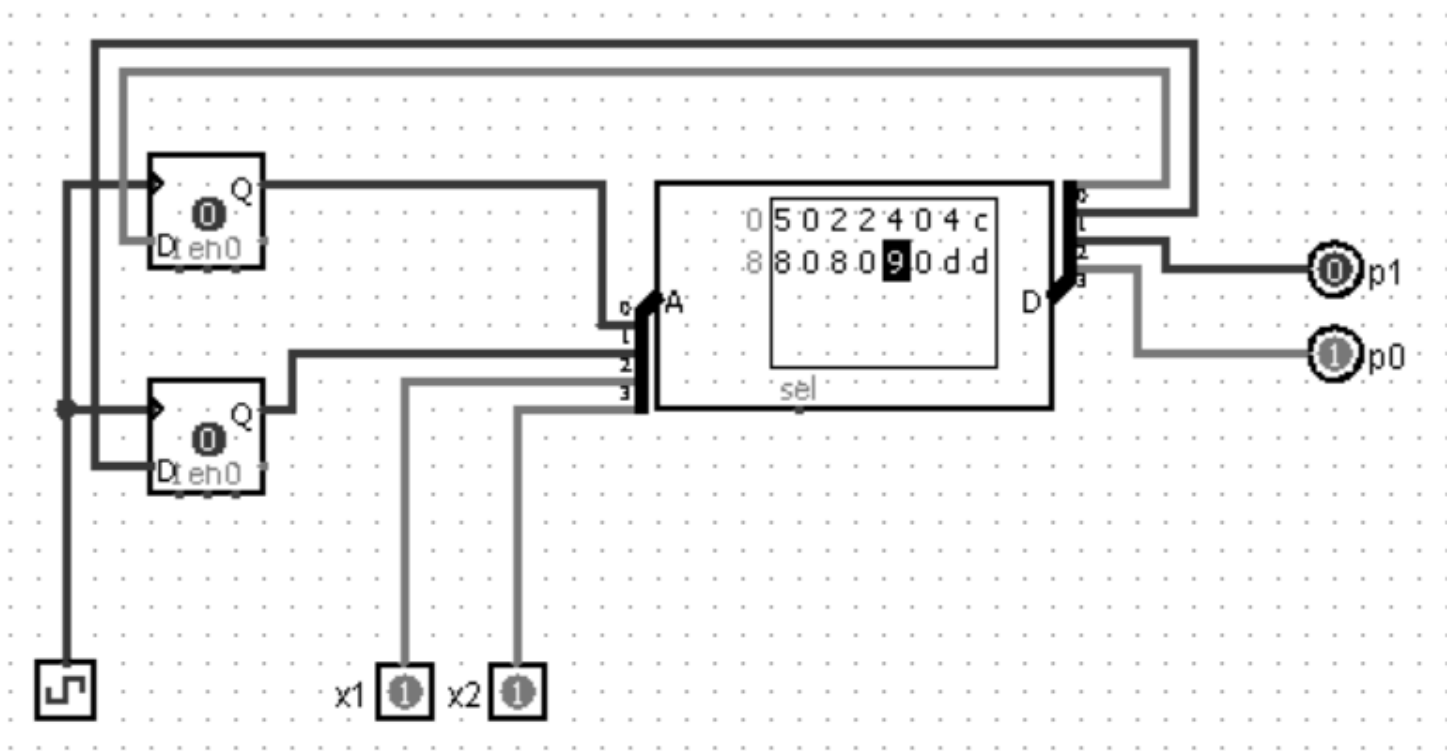
$Q_1^t Q_0^t$ \ $x_1x_2$		$x_1x_2$			
		00	01	11	10
$S_0$	01			00	00
$S_2$	01			11	01
$S_4$	10			11	11
$S_6$	10			00	10
		$Q_1^{t+1} Q_0^{t+1}$			

**Figure 5 - Encoded Karnaugh map used to obtain memory content.**

$Q_1^n$	$Q_0^n$	$x_1$	$x_2$	$Q_1^{n+1}$	$Q_0^{n+1}$	$P_1$	$P_0$
$A_3$	$A_2$	$A_1$	$A_0$	$Y_3$	$Y_2$	$Y_1$	$Y_0$
0	0	0	0	0	1	1	0
0	0	0	1	-	-	-	-
0	0	1	0	0	0	1	0
0	0	1	1	0	0	1	0
0	1	0	0	0	1	0	0
0	1	0	1	-	-	-	-
0	1	1	0	0	1	0	0
0	1	1	1	1	1	0	0
1	0	0	0	1	0	0	0
1	0	0	1	-	-	-	-
1	0	1	0	1	0	0	0
1	0	1	1	0	0	0	0
1	1	0	0	1	0	0	1
1	1	0	1	-	-	-	-
1	1	1	0	1	1	0	1
1	1	1	1	1	1	0	1

**Figure 6 - Memory content of microprogrammable circuit.**

Finally we connected the circuit and manually programmed the memory.



**Figure 7 - Circuit with implementation of the task.**

In the Logisim Hex Editor the memory content was written as:

6022 404c 8080 90dd

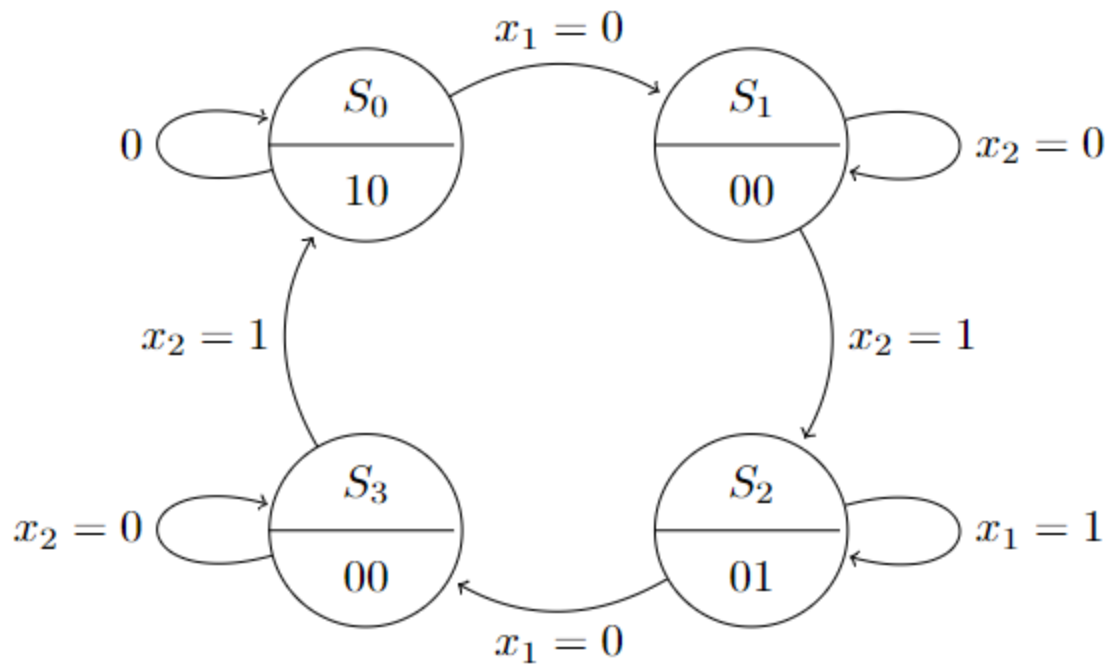
## Task 3

For the microprogrammable circuit obtain:

- Universal Structure
- Conditional Multiplexer-based Structure.**

## Solution

We created state diagram using table of memory content from previous task.



**Figure 9 - State diagram used to optimize memory size used.**

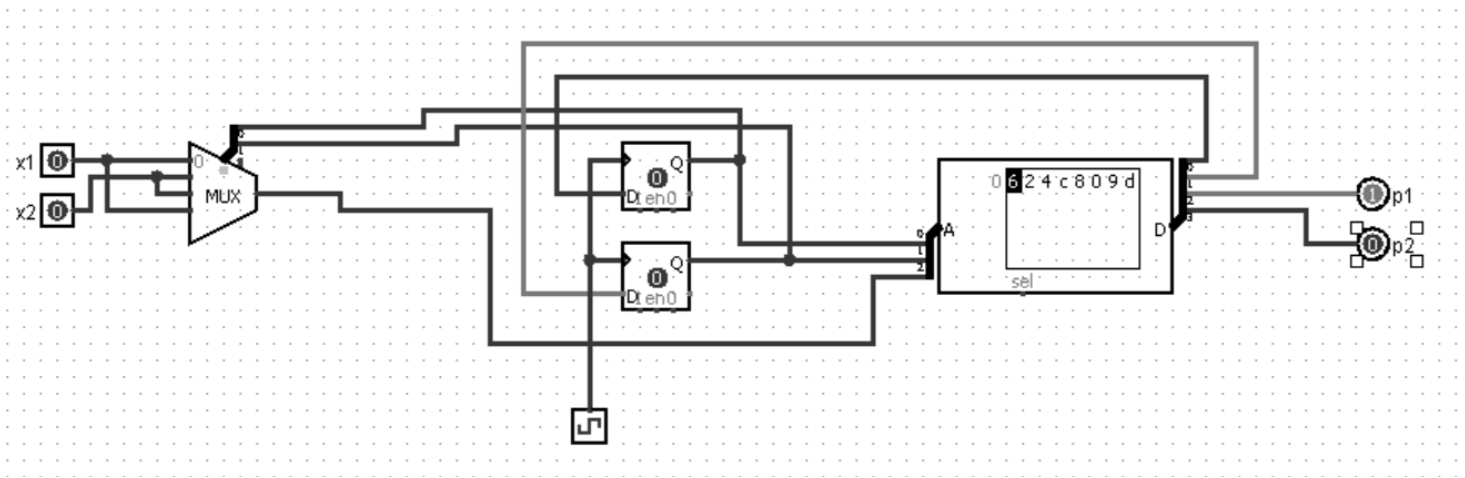
We noticed that each state change depends only on one variable. Using that information we created new table for the memory content.

$Q_1^n$	$Q_0^n$	$w^t$	$Q_1^{n+1}$	$Q_0^{n+1}$	$P_1$	$P_0$
$A_2$	$A_1$	$A_0$	$Y_3$	$Y_2$	$Y_1$	$Y_0$
0	0	0	0	1	1	0
0	0	1	0	0	1	0
0	1	0	0	1	0	0
0	1	1	1	1	0	0
1	0	0	1	0	0	0
1	0	1	0	0	0	0
1	1	0	1	0	0	1
1	1	1	1	1	0	1

**Figure 10 - Table of memory content of microprogrammable circuit.**

Finally we connected the circuit and manually programmed the memory.





**Figure 11 - Circuit with implementation of the task.**

In the Logisim Hex Editor the memory content was written as:

*624c 809d*

## Summary

The exercises successfully demonstrated the implementation of microprogrammable circuits. The following insights were gained:

- Microprogrammable circuits offer significant flexibility and reduced complexity in design.
- Optimization techniques, such as memory reduction, enhance efficiency without sacrificing functionality.